ABSTRACT

Selected data showing typical macroscopic residual stress distributions in u-bent Inconel 600, and 90 deg. bends in Incoloy 800 are presented. The results indicate regions of both high magnitude tension and compression in the longitudinal direction around the circumference of the bends at the apex.

The microscopic residual stress, or percent plastic strain and macroscopic residual distributions in the surface of cross-roll straightened and ground Inconel 600 tubing are described. The results indicate a compressive surface layer accompanied by a yield strength gradient from 90 ksi at the surface to 30 ksi at a depth of 0.003 in.

SAMPLE PREPARATION

The straight sample of Inconel 600 tubing which was employed for the study of the macroscopic residual stress and percent plastic strain (microstress) distributions as functions of depth was examined in the cross-roll straightened and ground condition as received from the mill. The straight tubing sample examined was nominally 0.625 in. in diameter with a 0.040 in. wall thickness. In the as-received condition, the 0.625 in. Inconel 600 tubing was reported to have a 0.2% yield strength of approximately 25 to 30 ksi.

An Inconel 600 2 1/2 in. u-bend sample was prepared from tubing having a nominal 0.75 in. O.D. and a 0.040 wall thickness. The u-bend sample was reportedly prepared from tubing in the mill annealed, cross roll straightened, and ground condition. The room temperature yield strength was assumed to be on the order of 25 to 30 ksi.

One sample of Incoloy 800 tubing with a nominal outside diameter of 1.00 in. and a 0.20 in. wall thickness was investigated. The sample was formed to a 90 deg./3D bend. The Incoloy 800 90 deg. bend sample was formed from material which was reportedly in the solution annealed and ground condition, with a yield strength on the order of 25 to 50 ksi.
EXPERIMENTAL METHOD

Subsurface Microscopic Residual Stress Distributions

The cross roll straightened and ground sample of 0.625 in. O.D./0.040 in. wall Inconel 600 tubing was employed to investigate the macroscopic and microscopic residual stress distributions as functions of depth to approximately 0.017 in. beneath the original ground surface. Both the microstress or degree of cold work and percent plastic strain, and the macroscopic residual stress were investigated so that both the state of macroscopic stress and the change in mechanical properties, such as yield strength, resulting from the plastic deformation which occurred during grinding could be determined.

Broadening of diffraction peaks as a result of plastic deformation resulting in disruption of the crystal lattice and increased dislocation density has been observed for years by many investigators. Line broadening data can be treated rigorously by the methods developed by Warren and Averbach \(^{(1)}\) to determine the contributions to peak broadening from crystallite size reduction, percent plastic strain, and instrumental broadening. A rigorous analysis of this type requires extensive data collection and exhaustive data reduction. Because the crystallite size contribution tends to be insignificant in the high back-reflection region, where data were collected for this investigation, and because the results could be obtained with fixed x-ray optics and slit systems providing a constant instrumental broadening, it appeared that simple measurement of the diffraction peak widths during the course of the measurement of macroscopic residual stress would suffice, provided an empirical relationship was established between the magnitude of the microscopic residual stress, or percent plastic strain, present in the samples and the diffraction peak width measured.

A technique for both macro- and microscopic residual stress measurement employing the diffraction of chromium K-β radiation from the (311) diffraction peaks was adopted in order to avoid complications arising from doublet separation when using the copper K-α technique normally employed for stress measurement in these alloys. Examples of the (311) diffraction peak obtained with chromium K-β radiation for a sample exhibiting approximately 15% plastic strain and one exhibiting approximately 40% plastic strain are shown in Figures 1 and 2, respectively.

An empirical relationship between the percent plastic strain on the surface of the sample and the FWHM of the (311) diffraction peak obtained with chromium K-β radiation was developed using samples of 0.625 in. diameter Inconel 600 tubing which were first annealed and then elongated in tension to known levels of plastic strain. The results and the calibration curve developed are shown in Figure 3. The angular width of the (311) diffraction peak was determined at two locations rotated 90 deg. around the circumference of the tubing samples employing both 1 deg. and 3 deg. divergent beams which resulted in approximately an order of magnitude increase in the diffraction peak intensity.
obtained. It was found that for tubing subjected to plastic strains of approximately 2, 4, 8, and 16%, a linear relationship was obtained between the width of the (311) diffraction peak and the plastic strain level. An attempt was made to subject a sample to 32% plastic strain, but necking resulted which is believed to be the cause of the deviation from a linear relationship. The strain level was also found to be significantly different between locations 1 and 2 measured on the 32% sample indicating nonuniform strain around the circumference. A discontinuity in the linear relationship was observed between 0% and 2% plastic strain. The same nonlinearity had been observed subsequently in data of this type developed for other nickel base alloys.

\[ \% p = 22.0(FWHM) - 20.3(\%) \]  

(1)

This relationship was then used to calculate the percent plastic strain as a function of depth in conjunction with the measurement of macroscopic residual stress.

**Macroscopic Residual Stress Measurement**

The macroscopic residual stress was determined in the 0.625 in. diameter Inconel 600 tubing sample at the surface and as a function of depth to nominally 0.017 in. beneath the sample surface in the direction parallel to the longitudinal axis of the tubing. X-ray diffraction residual stress measurements were made by the Two-Inclined Angle technique employing the diffraction of chromium K-β radiation from the (311) planes of the FCC structure of the Inconel 600 alloy. The diffraction peak angular positions were determined employing a five-point parabolic regression procedure after correction for the Lorentz-polarization an absorption effects, and for a linearly sloping background intensity.

The value of the elastic constants \( E/(1 + \nu) \) for the crystallographic direction normal to the (311) planes of the Inconel 600 alloy was determined experimentally in the course of the investigation by loading a simple rectangular beam manufactured from Inconel 600 in four-point bending on the diffractometer and determining the change in the lattice spacing of the (311) planes as a function of applied stress. The method employed to determine the x-ray elastic constants \( E/(1 + \nu) \) in the (311) direction required to calculate macroscopic residual stresses from strains measured in the crystal lattice has been described previously.

Material was removed for subsurface measurement by electropolishing in a sulfuric acid-methanol electrolyte minimizing possible alteration of the subsurface residual stress distribution as a result of material removal. The macroscopic residual stress data obtained as a function of depth were corrected for the effects of the penetration of the radiation employed for stress measurement into the subsurface stress gradient and for stress relaxation which occurred as a result of material removal.

X-ray diffraction residual stress measurements were made on the surface only of the u-bent Inconel 600 tubing sample in the longitudinal direction as a function of circumferential position around the u-bend apex. Measurements were made by the Two-Inclined Angle technique employing the diffraction of copper K-α radiation from the (420) planes. Residual stress measurements were made on the Incoloy 800 90-deg. bend sample in both the circumferential and longitudinal directions on the surface only at the apex of the bend by the Two Angle technique, employing the diffraction of chromium K-\( \alpha \) radiation from the (220) planes. For both the copper K-\( \alpha \) and chromium K-\( \alpha \) techniques, the x-ray elastic constants \( E/(1 + \nu) \) were determined empirically in the manner described above.
Because all measurements made on the bent tubing samples yielded surface data only, it was not possible to correct those results for the influence of the penetration of the radiation employed for stress measurement into the subsurface stress gradient.

Because of the geometry of the bends, only approximately a 1 in. length of the tubing could be mounted in the fixture, requiring sectioning of the bend samples. Electrical resistance strain gages attached to the surface of the bent tubing samples during the sectioning operation indicated stress relaxations in either the longitudinal or circumferential direction around the circumference of the tubing at the apex of the bend.

The results indicate compressive macroscopic residual stresses ranging from approximately -5 ksi at the surface to -21 at a depth of approximately 0.002 in. beneath the surface. The residual stress distribution then rises to cross the zero-stress axis approximately 0.005 in. beneath the surface. A peak tensile stress on the order of 8 ksi was observed at a depth of 0.010 in. beneath the surface, which diminished in magnitude with increasing depth.

The percent plastic strain was found to be approximately 16% at the surface and decreased exponentially as a function of depth to insignificant amounts at a depth of 0.005 in. beneath the surface.

The percent plastic strain as a function of depth can be expressed as a variation in yield strength with depth based upon the known stress-strain behavior for Inconel 600 tubing. Stress-strain relationships for Inconel 600 tubing are shown for total strain ranges of approximately 10%.
approximately 4% and 25% in Figures 6 and 7, respectively. It is apparent from the results shown in Figure 7 that Inconel 600 material which has been subjected 20% plastic strain would have a yield strength on the order of 100 ksi. This represents approximately a factor of 4 increase in yield strength compared to the original mill annealed condition.

The macroscopic residual stress, percent plastic strain, and the corresponding yield strength gradient based upon the data shown in Figures 6 and 7 are presented in Figure 8 on an expanded scale for the first approximately 0.003 in. beneath the ground surface of the straight Inconel 600 tubing. The results indicate a nearly linear decrease in yield strength with depth. The yield strength was found to range from approximately 95 ksi at a depth of 0.0001 in. beneath the surface to approximately 35 ksi, on the order of the mill annealed condition, at a depth of approximately 0.003 in.

The macroscopic residual stress results obtained in the longitudinal direction around the circumference of a single sample of 2 1/2 in. u-bent Inconel 600 tubing are presented in Figure 10. The data shown as open circles indicate the 0 to 180 deg. range. Measurements were
made near the neutral axis of the bend and near the extrados and intrados through the 180 to 360 deg. range and are shown as closed circles.

![Graph](image1)

**Fig. 10** - Longitudinal Residual Stress vs. (1+cos θ) Inconel 600, 2 ½ % In. U-Bend

The longitudinal results indicate generally tensile residual stresses ranging from the extrados to the neutral axis (1 + cos θ = 2.0 to 1.0) with maximum tensile stresses on the order of 15 to 30 ksi occurring in the neighborhood of (1 + cos θ) = 1.3. The stress distribution then changes very rapidly into compression near the neutral axis of the tubing achieving peak compressive stresses on the order of -85 ksi for (1 + cos θ) of approximately 0.7. The intrados of the bend was found to be approximately -20 ksi in compression. The compressive stress of -10 ksi measured at (1 + cos θ) = 2.0, the extrados, may be the result of a burnishing of the surface of the tubing which occurred during the bending operation.

The data shown in Figure 10 indicate an increase in yield strength of the surface layers, probably due to prior grinding, on the order of a factor of 3 greater than the mill annealed condition.

**Surface Longitudinal and Circumferential Residual Stresses on a 90 Deg./3D Bend in Incoloy 800 Tubing**

The longitudinal residual stress distribution around the circumference of the 1.00 in. diameter 90 deg./3D bend Incoloy 800 tubing sample are shown in Figure 11. The residual stress results show an oscillating pattern of stress entirely in tension from the extrados of the tubing to just beyond the neutral axis. Peak tensile stresses on the order of 80 ksi were observed immediately adjacent to the neutral axis. An extremely rapid change in stress was observed at the neutral axis, with peak compressive stresses on the order of -80 ksi occurring just below the point of transition at approximately (1 + cos θ) = 0.75. The region from the neutral axis to the intrados was found to be entirely compressive with approximately -20 ksi present on the intrados of the tubing.

![Graph](image2)

**Fig. 11** - Longitudinal Surface Residual Stress versus (1+ cos θ) Incoloy 800 Tubing, Sample B, Apex of Bend (φ = 0).

The oscillations observed in the longitudinal residual stress distribution from the extrados to the neutral axis may be the results of local variations in residual stress and yield strength as the result of work hardening caused by processing of the tubing prior to bending. Local stress variations of this type have been observed in the past on ground surfaces. The magnitude of the residual stress present on the surface of the tubing after bending indicates an increase in yield strength on the order of at least a factor of 2 for the surface layers of the Incoloy 800 tubing. It may be that the surface of the Incoloy 800 tubing prior to bending contained a residual stress and yield strength gradient not unlike that previously described for the straight sample of Inconel 600 tubing.

![Graph](image3)

**Fig. 12** - Circumferential Surface Residual Stress versus (1+COs θ) Incoloy 800 Tubing, Sample B, Apex of Bend (φ = 0)
The results obtained in the circumferential direction at the apex of the 90 deg./3D bend are presented in Figure 12. The results show entirely compressive stresses from the extrados to the neutral axis with a peak compressive value on the order of -50 ksi occurring at approximately \((1 + \cos \theta) = 1.6\). Oscillations similar to those observed in the longitudinal direction occur from the extrados to the neutral axis in the circumferential direction. The circumferential residual stress distribution becomes tensile from the neutral axis to near the intrados with a nearly constant stress distribution on the order of 15 to 20 ksi. The intrados was found to be approximately -25 ksi in compression, which may be the result of local deformation or burnishing during the bending operation.

CONCLUSIONS

The results shown for the subsurface residual macroscopic and microscopic residual stresses produced by grinding straight 0.625 in. diameter Inconel 600 tubing indicate increases in yield strength from nominally 30 to 90 ksi at the ground surface. The yield strength gradient diminishes nearly linearly to reach the nominal mill annealed value of approximately 30 ksi at a depth of 0.003 in. The residual stress distribution associated with the grinding operation was found to be entirely compressive to a depth of approximately 0.005 in., with low magnitude tensile stresses beneath.

Examination of a 0.75 in. O.D. Inconel 600 tubing 2 1/2 in. u-bend shows entirely compressive stresses reaching magnitudes as high as -85 ksi from the intrados to the neutral axis, and tensile stresses reaching 20 ksi from the neutral axis to the extrados. An extremely large stress gradient exists in the vicinity of the neutral axis.

An even larger stress gradient exists in the vicinity of the neutral axis, and higher magnitude tension and compression, on the nominally 1 in. diameter Incoloy 800 90 deg./3D bend were examined. Oscillations observed in the stress pattern in both the longitudinal and circumferential directions at the surface may be the result of variations in surface residual stress and yield strength caused by grinding the surface prior to forming the bend.

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